

# Secure Information Flow

## Program Slicing

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Winter Term 2014/15

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Advanced Lecture (9 CP)

Christian Hammer



## Program Slicing in the PDG

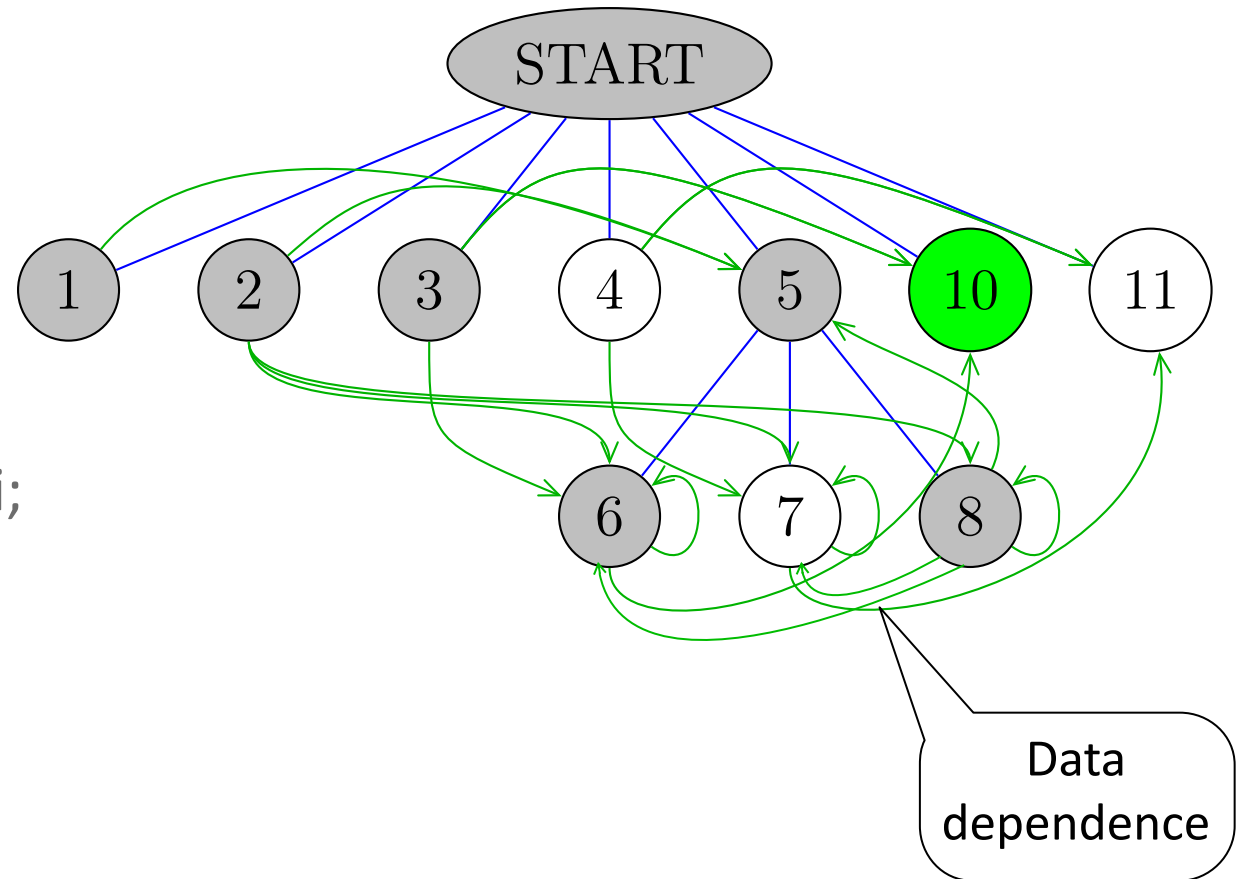
- Which statements can influence the the slicing criterion?
- Defined slightly different from Weiser's original
- Slicing criterion is just a node  $v$  in the dependence graph
- Equivalent to criterion  $(v, \text{Ref}(v) \cup \text{Def}(v))$
- **Intraprocedural Backward Slice:**  
$$\text{BS}(v) = \{x \in \text{PDG} \mid x \rightarrow^* v\}$$
- Simple graph-reachability problem based on transitivity of data and control dependence

## Example for Backwards Slice

```
(1)  read(n);
(2)  i = 1;
(3)  sum = 0;
(4)  prod = 1;
(5)  while (i <= n) {
(6)    sum = sum + i;
(7)    prod = prod * i;
(8)    i++;
(9)  }
(10) write(sum);
(11) write(prod);
```

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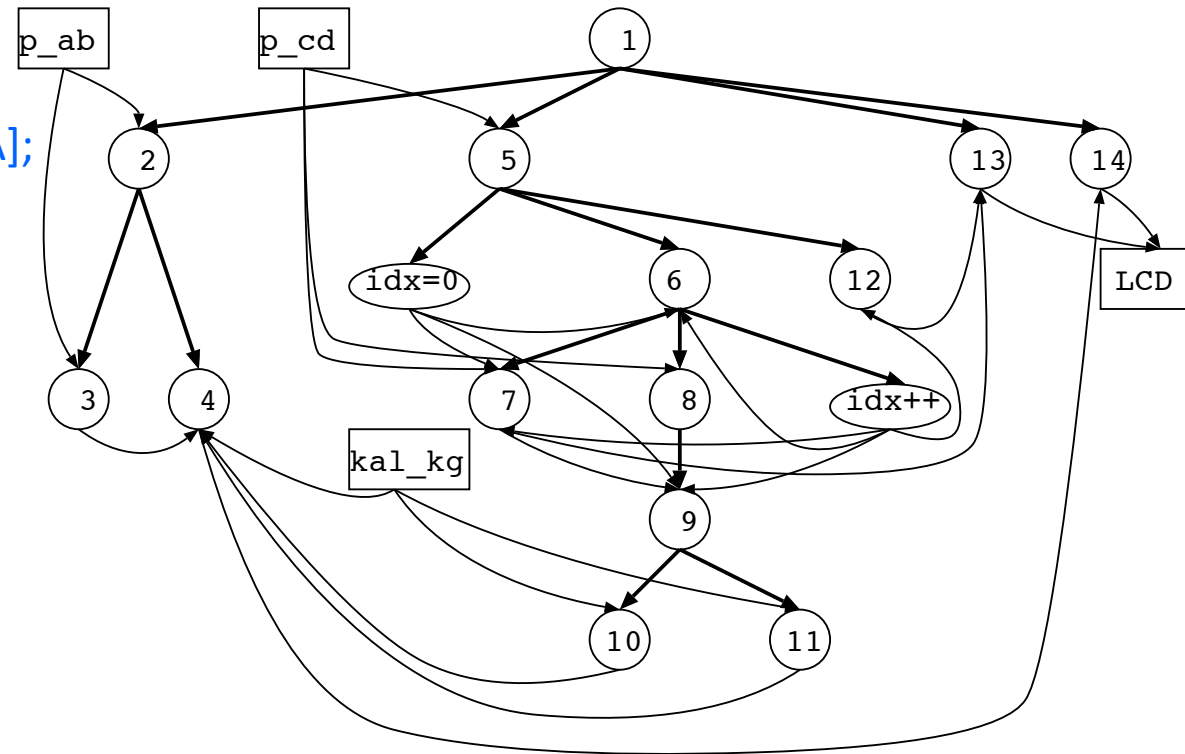


## Correctness of Slicing

- Theorem:  
A backward slice from a node  $v$  contains all the statements that could potentially influence the computation of variables defined or used at  $v$ .
- Proof: Wasserrab PhD, formalized in Isabelle

## Scale

```
(1) while(TRUE) {  
(2)   if ((p_ab[CTRL2] & 0x10)==0) {  
(3)     u = ((p_ab[PB] & 0x0f) << 8) + p_ab[PA];  
(4)     u_kg = u * kal_kg;}  
(5)   if ((p_cd[CTRL2] & 0x01) != 0) {  
(6)     for (idx=0;idx<7;idx++) {  
(7)       e_puf[idx] = p_cd[PA];  
(8)       if ((p_cd[CTRL2] & 0x10) != 0) {  
(9)         switch(e_puf[idx]) {  
(10)          case '+': kal_kg *= 1.1; break;  
(11)          case '-': kal_kg *= 0.9; break; } }  
(12)       e_puf[idx] = '\0'; }  
(13)   printf("Artikel: %07.7s\n",e_puf);  
(14)   printf(" %6.2f kg ",u_kg);  
(15)}
```



## Scale

```
(1) while(TRUE) {
(2)   if ((p_ab[CTRL2] & 0x10)==0) {
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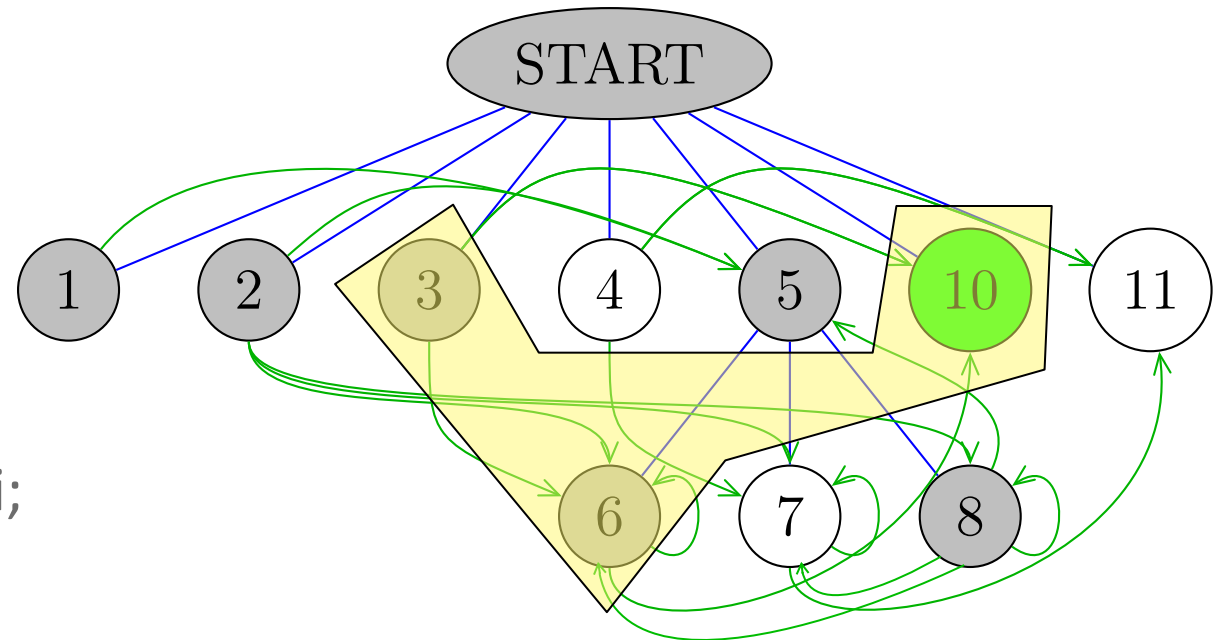
## Forward Slicing

- Backward slicing: which statements can influence the the slicing criterion?
- Forward slicing: which statement can be influenced by the slicing criterion?
- **Intraprocedural Forward Slice:**  
$$FS(v) = \{x \in PDG \mid v \rightarrow^* x\}$$
- What is transitively reachable from the slicing criterion?



## Example

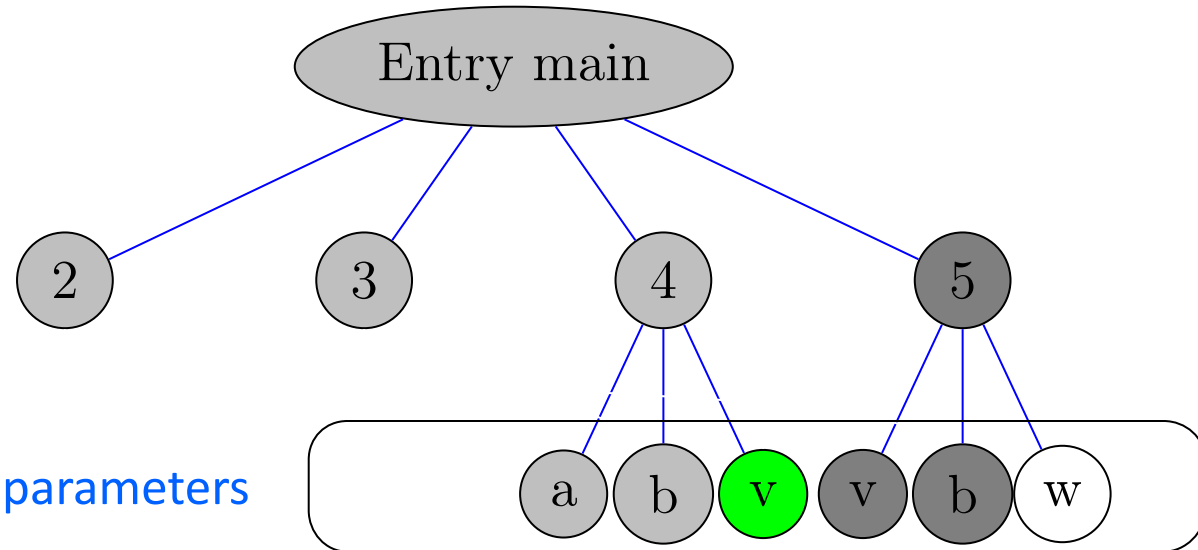
```
(1) read(n);  
(2) i = 1;  
(3) sum = 0;  
(4) prod = 1;  
(5) while (i <= n) {  
(6)   sum = sum + i;  
(7)   prod = prod * i;  
(8)   i++;  
(9) }  
(10) write(sum);  
(11) write(prod);
```



## Interprocedural Analysis

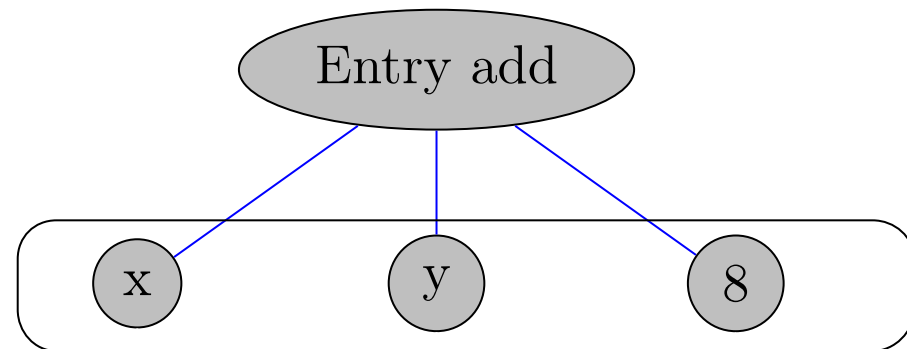
```
1 main() {  
2   a=3;  
3   b=4;  
4   v=add(a,b);  
5   w=add(v,b);  
6 }  
7 add(x,y) {  
8   return x+y;  
9 }
```

Actual parameters







— control dependence

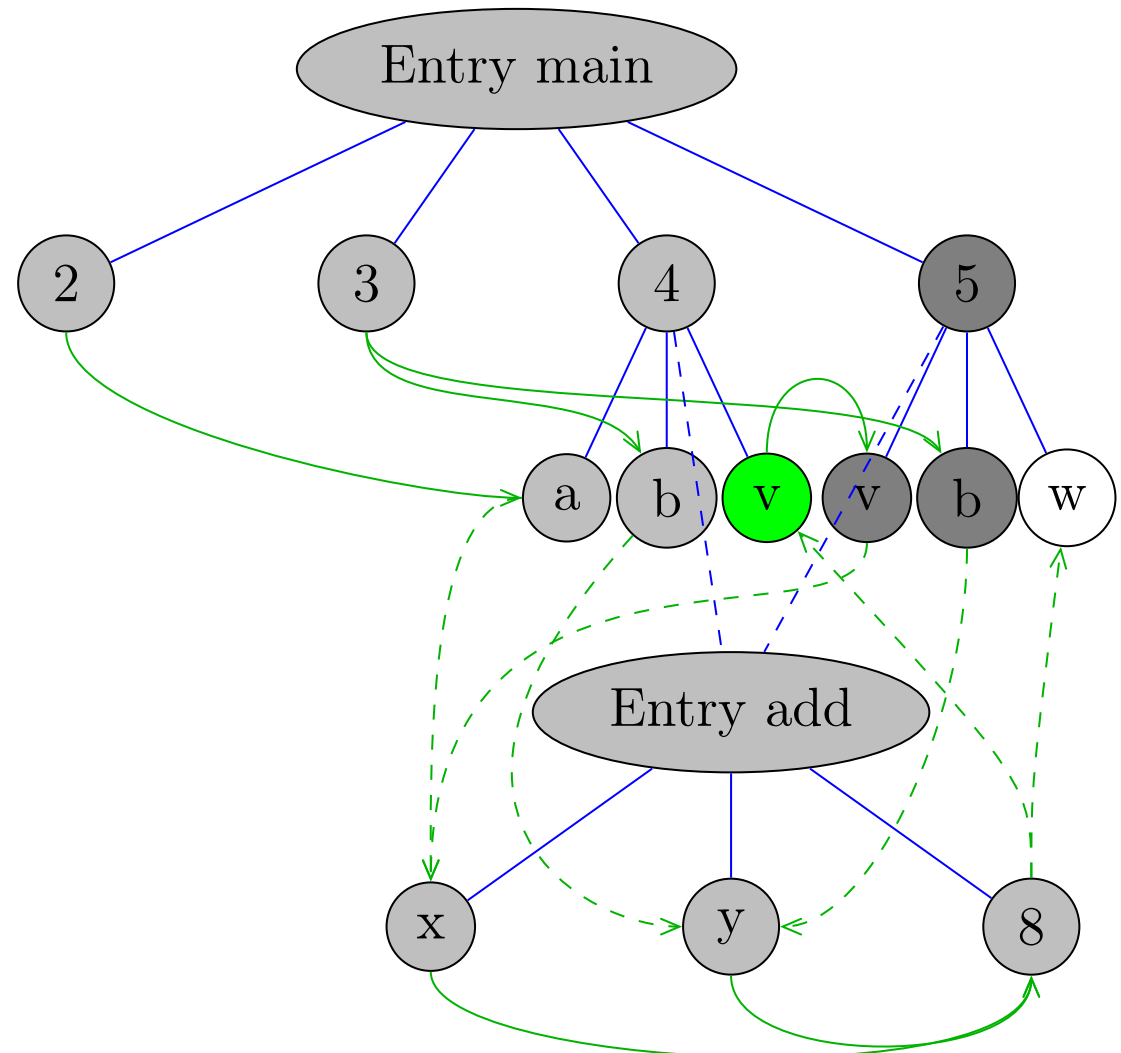
Formal parameters



## Interprocedural Analysis: Parameter Passing

```
1 main() {  
2   a=3;  
3   b=4;  
4   v=add(a,b);  
5   w=add(v,b);  
6 }  
7 add(x,y) {  
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9 }
```

-  data dependence
-  control dependence
-  parameter edges
-  call dependence



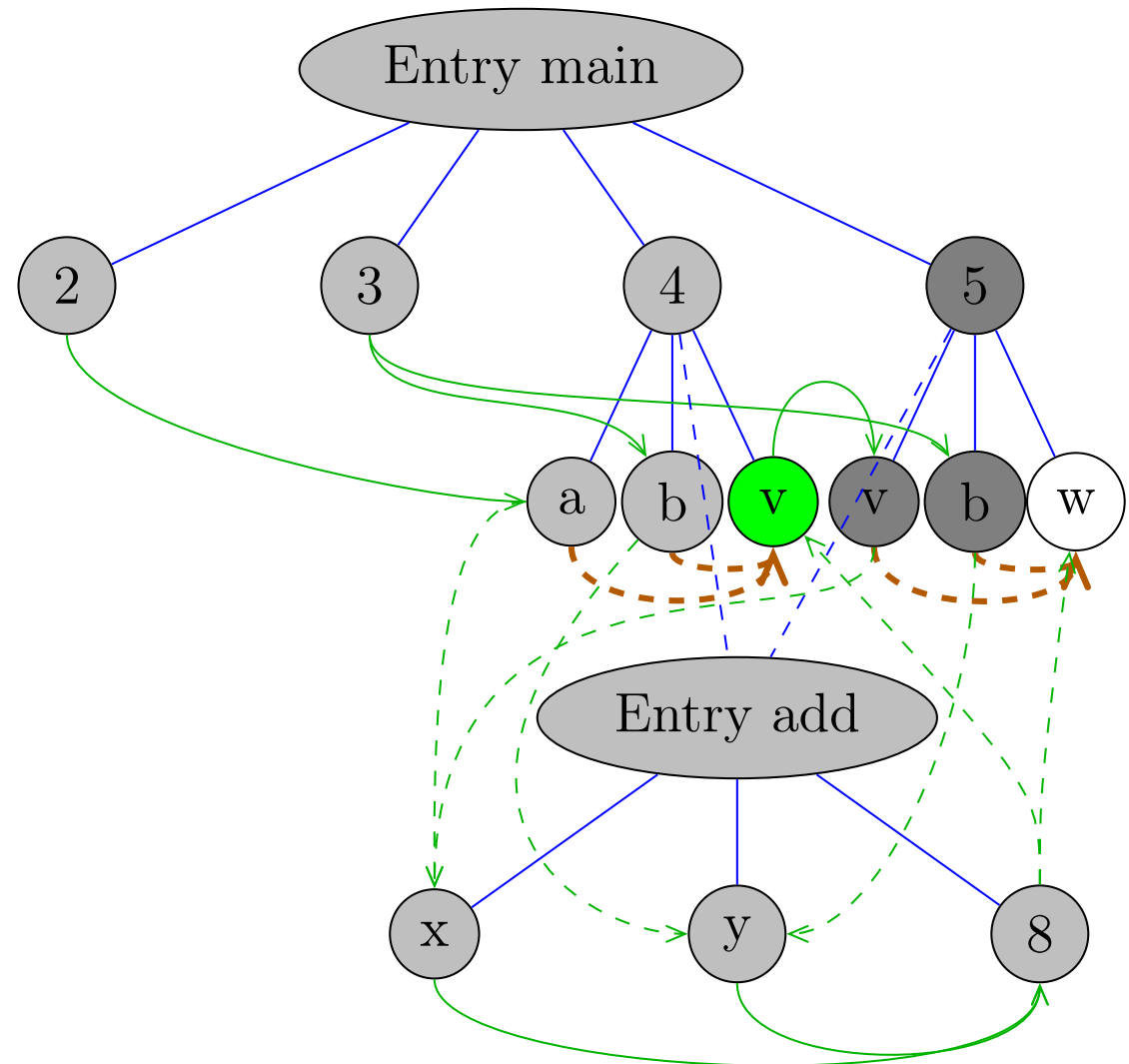
## Interprocedural Slicing

- Backward slicing from  $v$  would contain the whole graph except for  $w$ .
- But 5 and its children are not influencing the definition of  $v$  in line 4.
- This is called context-insensitive program slicing.
- It may contain **spurious nodes** (imprecise, in dark grey)
- Idea: only return to same call site where we left the method

## Interprocedural Analysis: Summary Edges

```
1 main() {  
2   a=3;  
3   b=4;  
4   v=add(a,b);  
5   w=add(v,b);  
6 }  
7 add(x,y) {  
8   return x+y;  
9 }
```

- data dependence
- control dependence
- - - → summary edge
- - - → parameter edges
- - - → call dependence



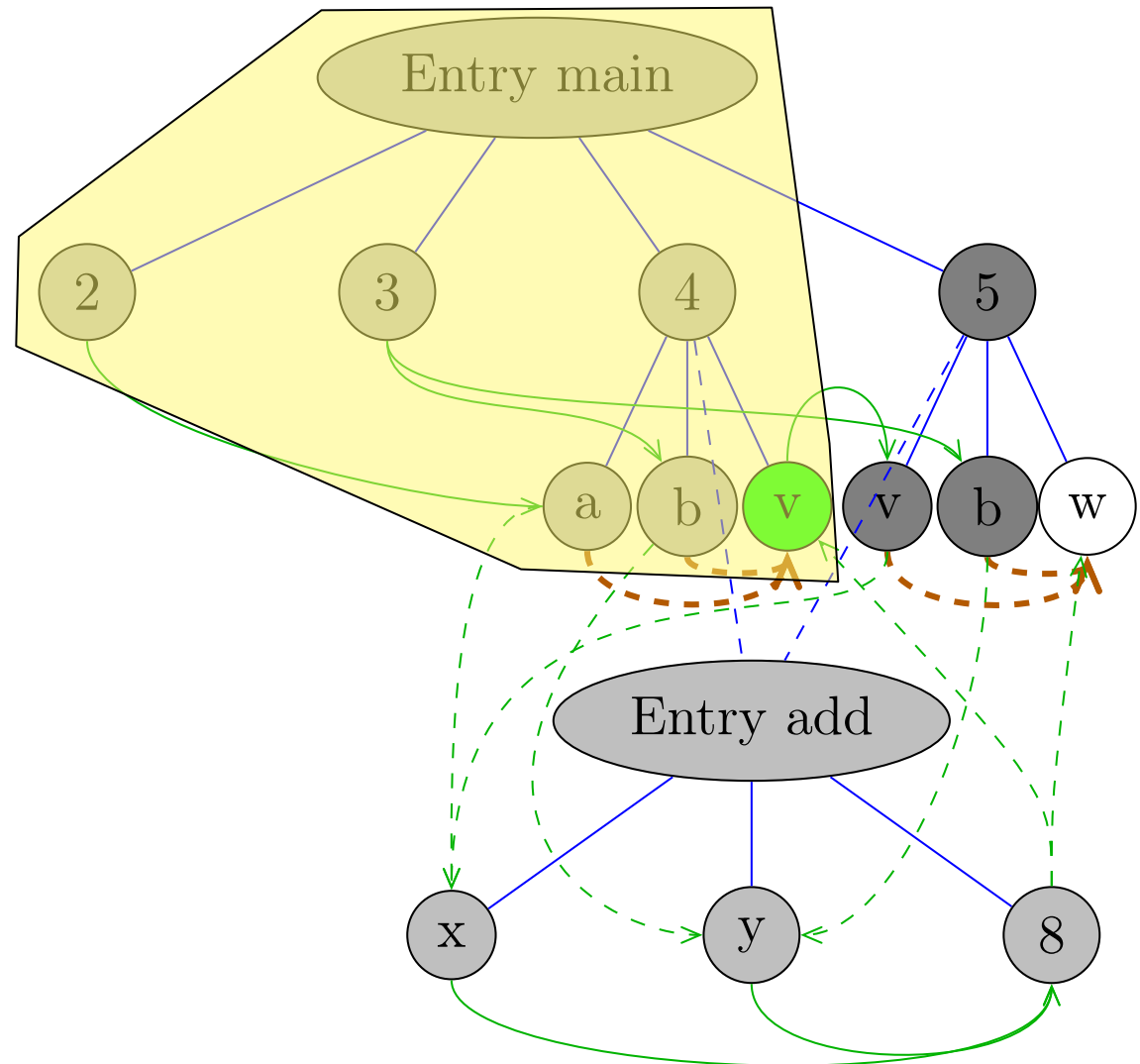
## Two-Phase Slicing

- In the first phase:  
Do not descend into called methods, mark omitted edges for later phase. Traverse summary edges instead.
- In the second phase:  
Starting with the omitted edges, do not reascend into calling method. Still traverse summary edges.

## Interprocedural Analysis

```
1 main() {  
2   a=3;  
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5   w=add(v,b);  
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7 add(x,y) {  
8   return x+y;  
9 }
```

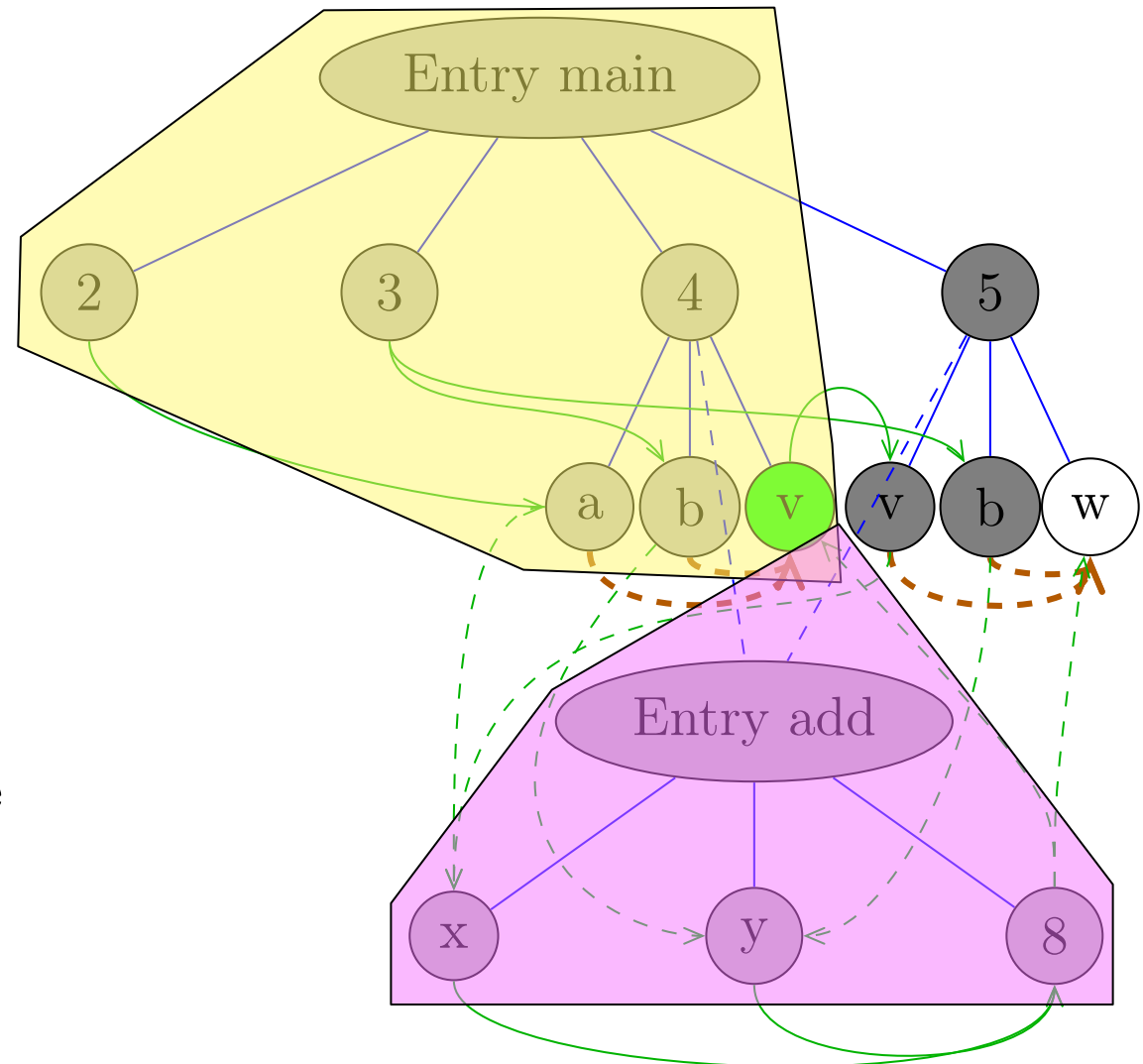
- data dependence
- control dependence
- - - -> summary edge
- - - -> parameter edges
- - - -> call dependence



## Interprocedural Analysis

```
1 main() {  
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9 }
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- data dependence
- control dependence
- summary edge
- parameter edges
- call dependence





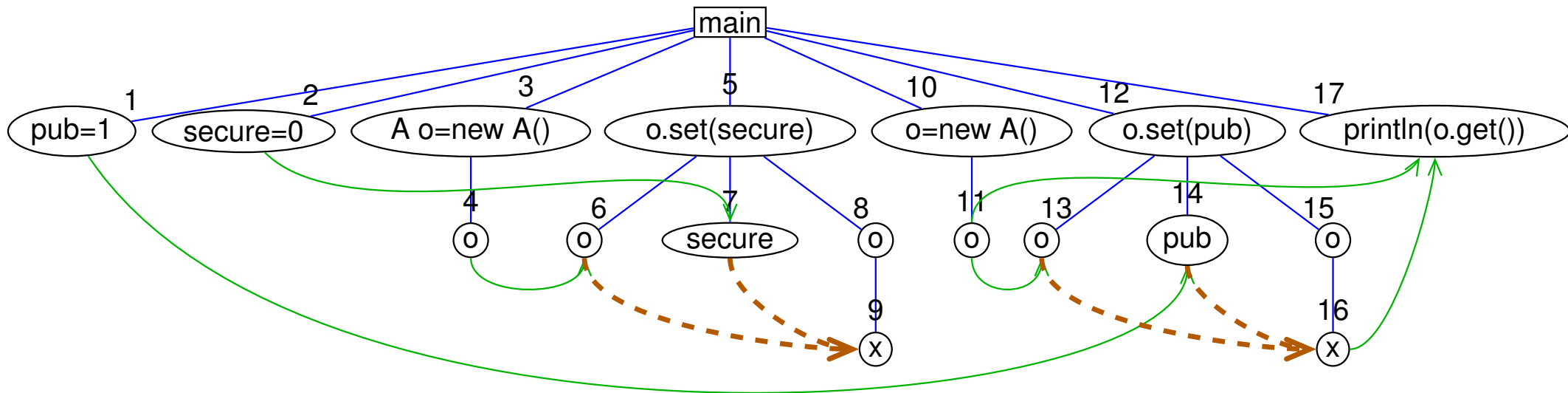
```
W =  $\emptyset$ , worklist
P =  $\emptyset$ 
foreach  $n \in N$  which is a formal-out node do
  W =  $W \cup \{(n, n)\}$ 
  P =  $P \cup \{(n, n)\}$ 
Iteration
while  $W \neq \emptyset$  worklist is not empty do
  W =  $W / \{(n, m)\}$  remove one element from the worklist
  if n is a formal-in node then
    foreach  $n' \xrightarrow{pi} n$  which is a parameter-in edge do
      foreach  $m \xrightarrow{po} m'$  which is a parameter-out-edge do
        if  $n'$  and  $m'$  belong to the same call site then
          E =  $E \cup n' \xrightarrow{su} m'$  add a new summary edge
          foreach  $(m', x) \in P \wedge (n', x) \notin P$  do
            P =  $P \cup \{(n', x)\}$ 
            W =  $W \cup \{(n', x)\}$ 
        else
          foreach  $n' \xrightarrow{dd, cd, su} n$  do
            if  $(n', m) \notin P$  then
              P =  $P \cup \{(n', m)\}$ 
              W =  $W \cup \{(n', m)\}$ 
    return G the SDG
```

## Example Program

```
(1) class A {
(2)   int x;
(3)   void set() { x = 0; }
(4)   void set(int i) { x = i; }
(5)   int get() { return x; }
(6) }
(7) class B extends A {
(8)   void set() { x = 1; }
(9) }

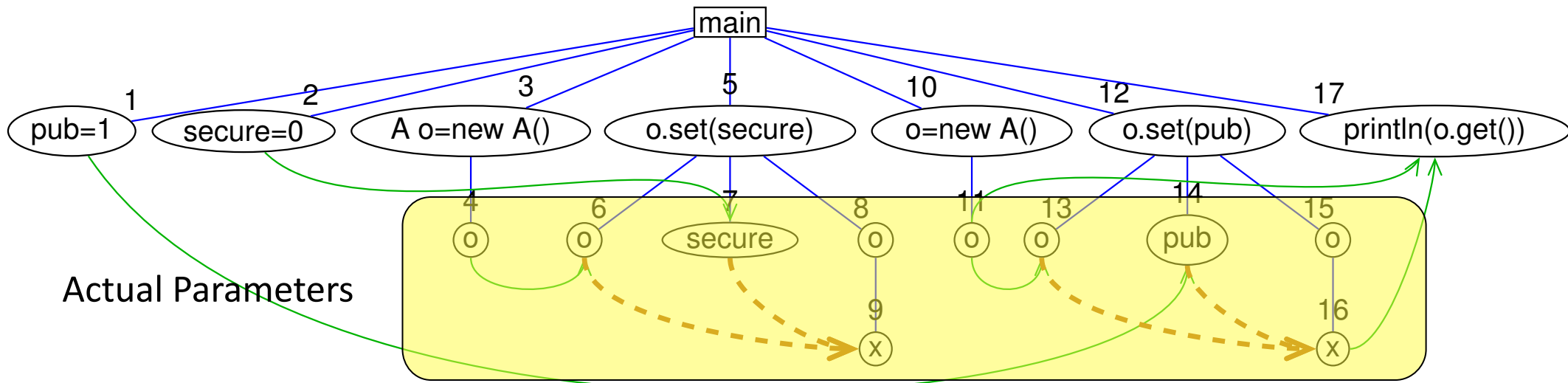
(11) class InFlow {
(12) static void main(String[] a) {
(13)   // 1: no information flow
(14)   int sec = 0, pub = 1;
(15)   A o = new A();
(16)   o.set(sec);
(17)   o = new A();
(18)   o.set(pub);
(19)   System.out.println(o.get());
(21)   // 2: dynamic dispatch
(22)   if (sec==0 && a[0].equals("007"))
(23)     o = new B();
(24)   o.set();
(25)   System.out.println(o.get());
(27)   // 3: instanceof
(28)   o.set(42);
(29)   System.out.println(o instanceof B);
(30)}}
```

## SDG for first part of the Program



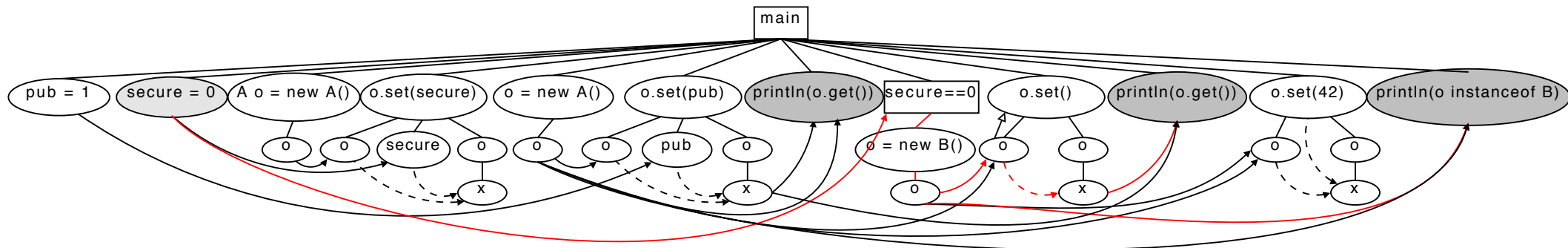
- **Summary edges** for transitive flow of parameters
- Allows context-sensitive slicing
- Object-sensitive slice of first `println(o.get())` does *not* contain `secure`
- Program part is guaranteed to be secure (noninterferent)

## SDG for first part of the Program



- **Summary edges** for transitive flow of parameters
- Allows context-sensitive slicing
- Object-sensitive slice of first `println(o.get())` does *not* contain `secure`
- Program part is guaranteed to be secure (noninterferent)

## SDG for complete Program



- Slice from second `println(o.get())` contains `secure`
- Slice from `instanceof` also contains `secure`
- Both parts of the program potentially insecure
- Input “007” triggers illegal flow

## References

- Hammer, C. [Information Flow Control for Java - A Comprehensive Approach based on Path Conditions in Dependence Graphs](#). Ph.D. Thesis, Universität Karlsruhe (TH), Fak. f. Informatik, 2009. (also available at the CS Library)



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